

# nflWAR: A Reproducible Method for Offensive Player Evaluation in Football

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# Reproducible Research with nflscrapR

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## nflscrapR:

- R package created by Maksim Horowitz to enable easy data access and promote reproducible NFL research
- Collects play-by-play, game, roster data from NFL.com
- Data is available for all games starting in 2009 (soon 1998!)

## Available on Github, install with:

```
devtools::install_github(repo=maksimhorowitz/nflscrapR)
```

# Principles of nflWAR

- Publicly available data, code, and results; **reproducible**
- Interpretable in terms of game outcomes (e.g points, wins)
- Account for uncertainty (football is a small sample game)
- Allow for objective decision-making by coaches/management

# Our nflWAR Framework

- Create **open-source software** for the collection of NFL data  
see R package `nflscrapR` – Horowitz, Yurko, Ventura (2017)
- Properly model plays to determine **play value**
- Use play valuations to model **player value**
- Make player evaluation results **useful and interpretable**:
  - Evaluate relative to replacement level
  - Convert to a wins scale
  - Estimate the uncertainty in our evaluations of players

# How to Value Plays?



Suppose it's 4th down with 4 yards to go from the 40 yard line.

You have three choices:

- **Punt:**

You are sacrificing possession, but gaining (some) field position

- **Attempt a field goal:**

You are sacrificing possession, but (possibly) gaining three points

- **“Go for it”:**

You try to advance the ball four yards to maintain possession

# How to Value Plays?

**Expected Points (EP):** Value of play is in terms of  $E(\text{points of next scoring play})$

- How many points have teams scored when in similar situations? (yard line, down, yards to go, etc.)
- Several ways to model this
- **Our approach: multinomial logistic regression**

**Win Probability (WP):** Value of play is in terms of  $P(\text{Win})$

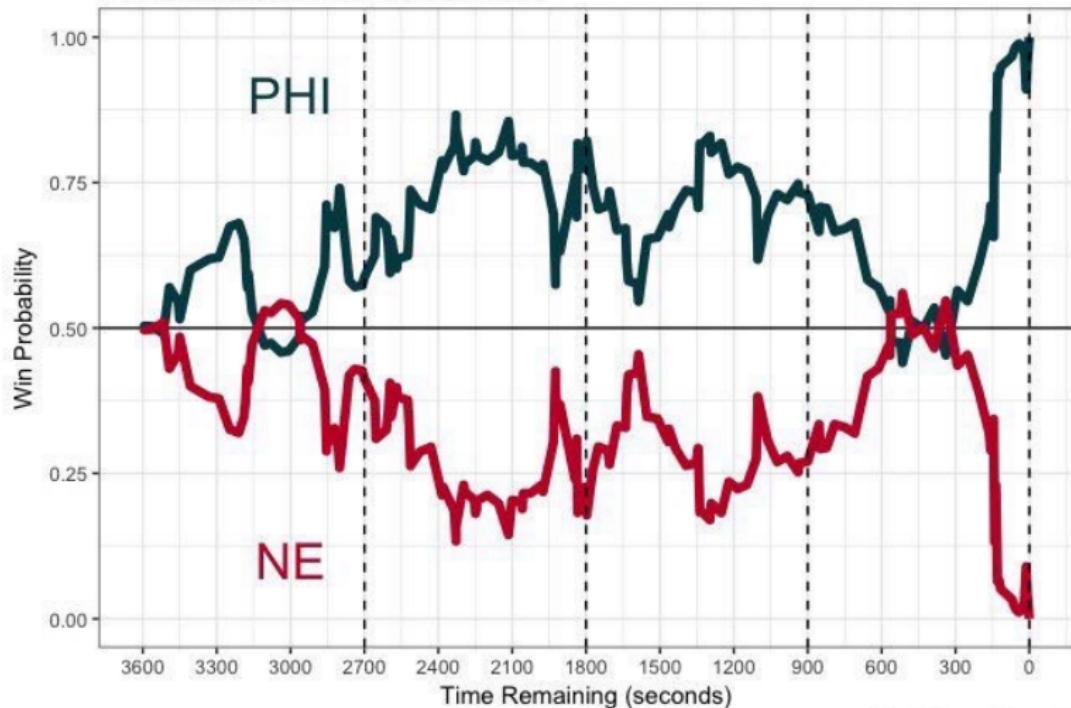
- Have teams in similar situations won the game?
- Common approach is logistic regression
- **Our approach: generalized additive model (GAM)**

Can apply **nflWAR** framework to both (or any measure of play value)

# Superbowl LII Win Probability Chart

## Super Bowl LII Win Probability Chart

Philadelphia Eagles vs. New England Patriots



Data from nflscrapR

# Estimating the Value of a Play



Win Probability Added (**WPA**) or Expected Points Added (**EPA**)  
Using **air yards** → **airWPA/airEPA** and **yacWPA/yacEPA**

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Comment from Pittsburgh Post-Gazette article on `nflscrapR`

stats dont work as well in football as compared to other sports such as baseball. you cant statistically evaluate a running back without evaluating his offensive line. same thing with a QB. you cant evaluate a QB without evaluating his receivers (drop balls, wrong route etc). stats can only be helpful when an athlete is doing something completely on his own (pitching). that is why the nfl doesnt go crazy over stats--it's a team sport on every single play. the only stat that counts is the W.

[Reply](#)

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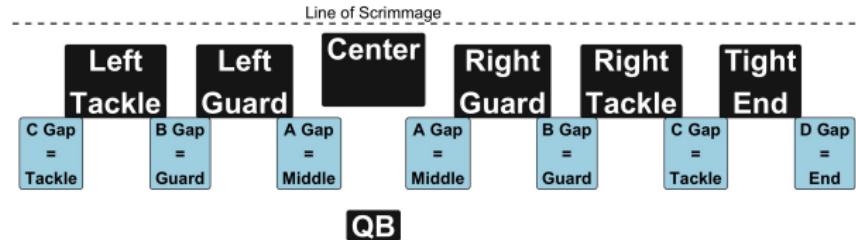


**Football is complex, need to divide credit, evaluate using wins!**

# Division of Credit

**Publicly available data only includes those directly involved:**

- Passing:
  - Players: passer, targeted receiver, tackler(s), and interceptor
  - Context: air yards, yards after catch, location (left, middle, right), and if the passer was hit on the play
- Rushing:
  - Players: rusher and tackler(s)
  - Context: run gap (end, tackle, guard, middle) and direction (left, middle, right)



# Multilevel Modeling

Growing in popularity (and rightfully so):

- “Multilevel Regression as Default” - Richard McElreath
- Natural approach for data with **group structure**, and different levels of variation within each group
  - e.g. QBs have more pass attempts than receivers have targets
- Every play is a repeated measure of performance
- Hockey example: WAR-on-ice (*Thomas et al., 2013*)
- Baseball example: Deserved Run Average (*Judge et al., 2015*)

# Multilevel Modeling

Example of **varying-intercept** model:

$$WPA_i \sim \text{Normal}(Q_{q[i]} + C_{c[i]} + X_i \cdot \beta, \sigma_{WPA}^2), \text{ for } i = 1, \dots, n \text{ plays}$$

Key feature is the **groups are given a model** - treating the levels of groups as similar to one another with **partial pooling**

$$Q_q \sim \text{Normal}(\mu_Q, \sigma_Q^2), \text{ for } q = 1, \dots, \# \text{ of QBs},$$

$$C_c \sim \text{Normal}(\mu_C, \sigma_C^2), \text{ for } c = 1, \dots, \# \text{ of receivers.}$$

Unlike linear regression, no longer assuming independence

Provides estimates for **average play effects** while providing necessary **shrinkage** towards the group averages

# nflWAR Modeling

Use varying-intercepts for each of the grouped variables

With location and gap, create **Team-side-gap** as O-line proxy  
e.g. PIT-left-end, PIT-left-tackle, PIT-left-guard, PIT-middle

Separate passing and rushing with different grouped variables

- Passing: Quarterback, receiver, defensive team
- Rushing: Team-side-gap, rusher, defensive team

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- Passing: Quarterback, receiver, defensive team
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Each group intercept is an estimate for an individual or team effect,

- **individual points/probability added (iPA)**
- **team points/probability added (tPA)**

Multiply intercepts by attempts to get **points/probability above average (iPAA/tPAA)**

# nflWAR Modeling

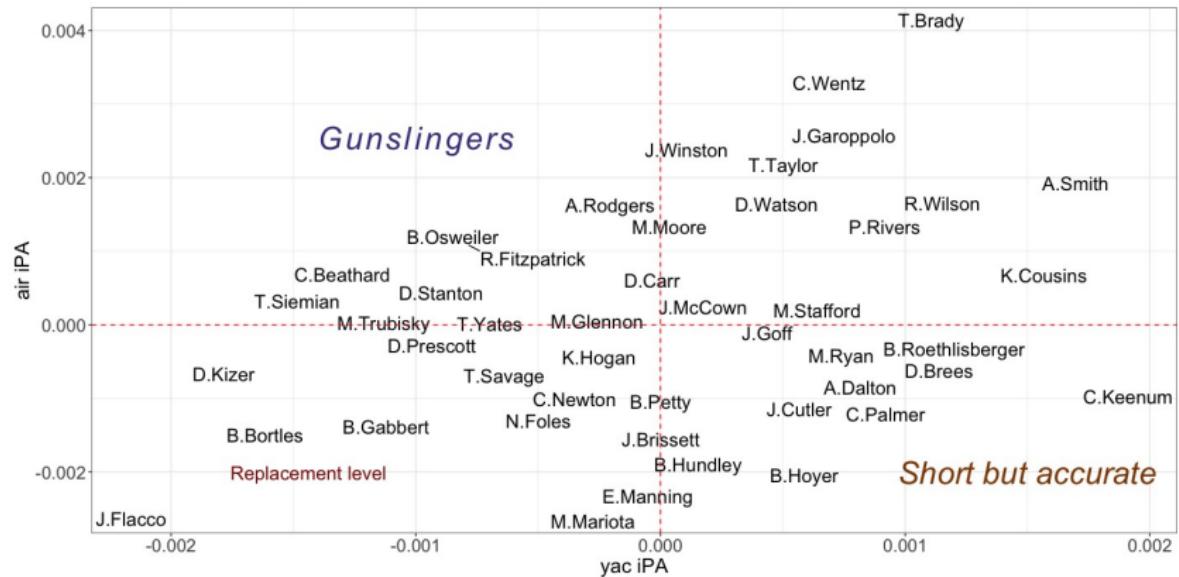
Four different models to measure three skills:

- Two separate models for QB and non-QB **rushing**
- Two separate passing models for **air** and **yac**

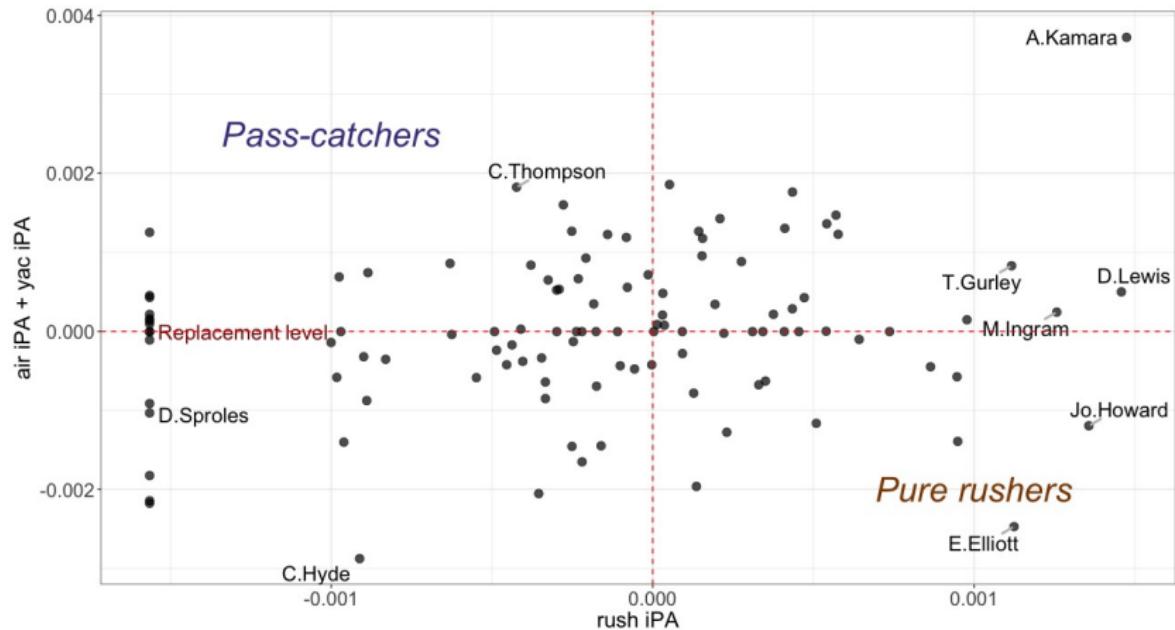
Models adjust for team strength using opposite type of EPA per attempt (e.g. rushing models adjust for passing strength)

Every player has  $iPA_{rush}$ ,  $iPA_{air}$ , and  $iPA_{yac}$  estimates

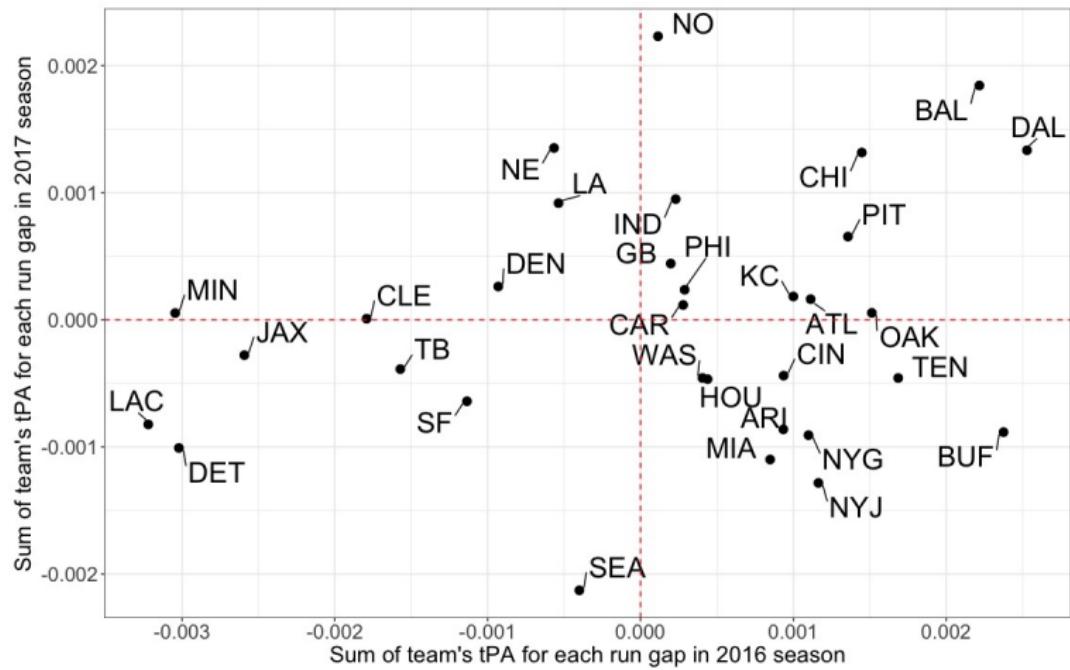
## QB Air vs Yac Efficiency in 2017



# RB Receiving vs Rushing Efficiency in 2017



# Comparing Team Offensive Line Performance 2016-17



# Arriving at WAR

Evaluate relative to “shadow” replacement player based on rosters similar to **openWAR** (Baumer et al., 2015)

Results in **individual points above replacement (iPAR)**

Convert points to wins using regression approach

$$\text{Points per Win} = \frac{1}{\hat{\beta}_{\text{Score Diff}}}$$

Two types of *WAR*:

$$\text{EPA-based } \textit{WAR} = \frac{\textit{iPAR}}{\text{Points per Win}}$$

$$\text{WPA-based } \textit{WAR} = \textit{iPAR}$$

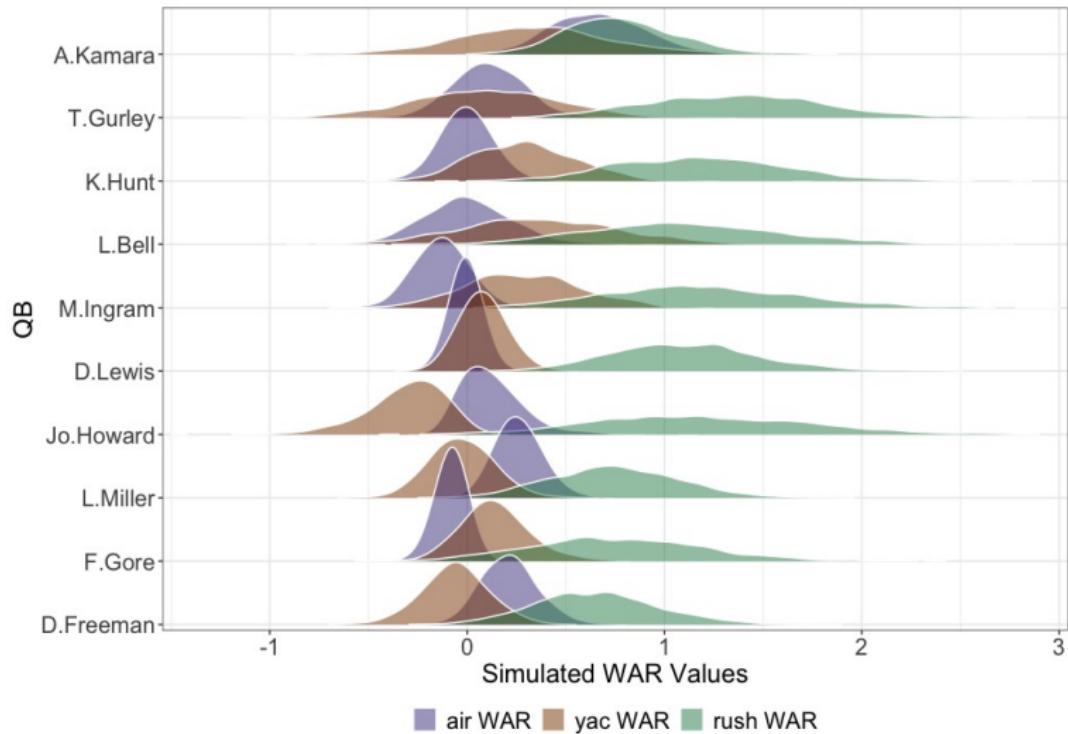
# Uncertainty is Mandatory

Similar to **openWAR** (again!) we use a resampling strategy to generate *WAR* distributions

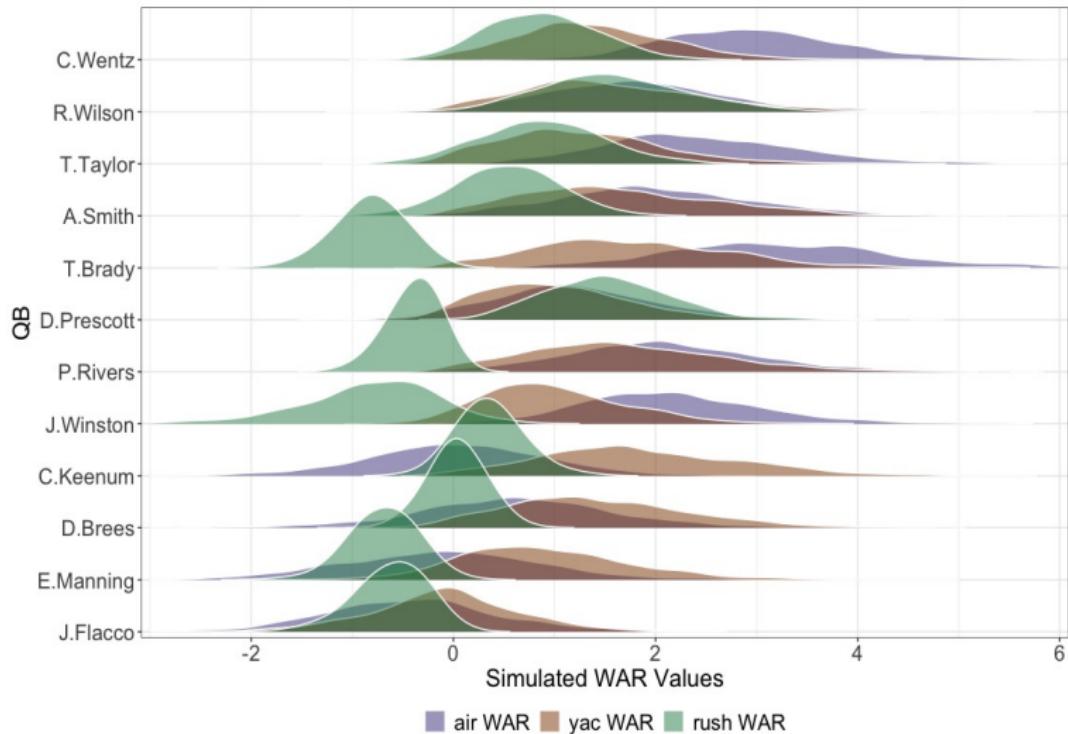
We resample **entire team drives** to preserve any play-sequencing tendencies that could affect our estimates

Following estimates are based on 1000 simulations

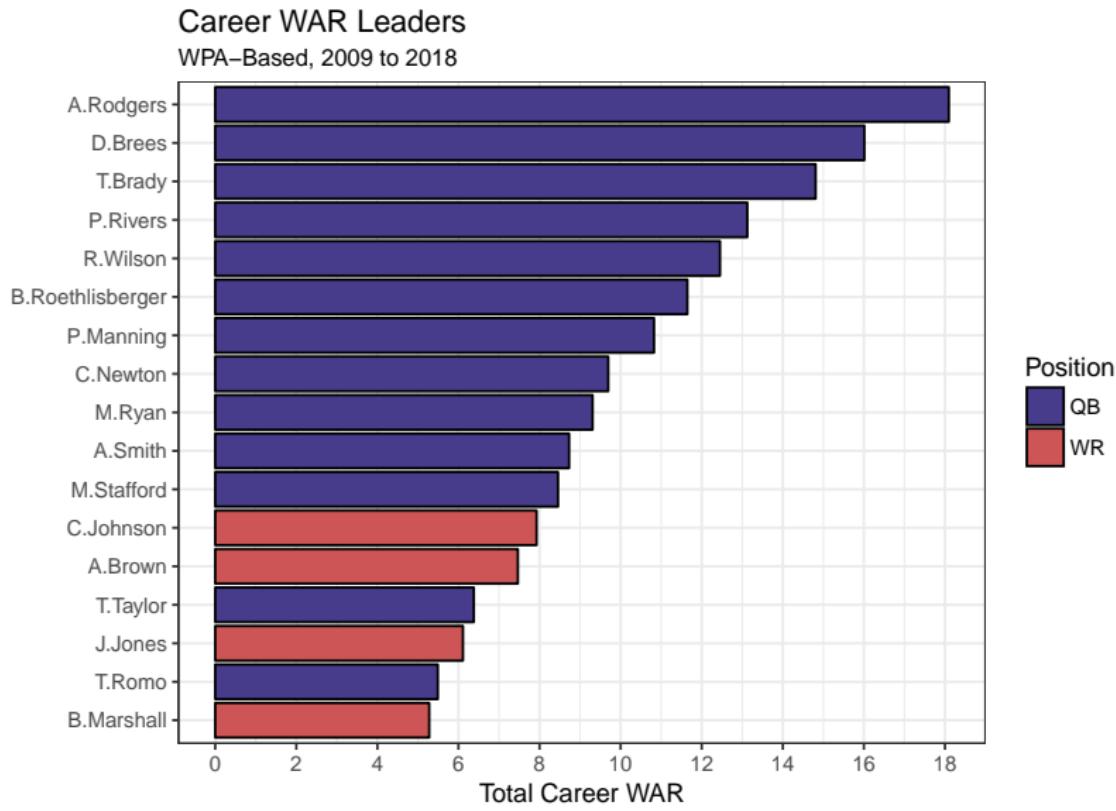
# Top RBs by WAR in 2017



# Selection of QB WAR Distributions in 2017



# Career WAR Leaders



Data from NFL.com via nflscrapR; WAR from <https://github.com/ryurko/nflscrapR-data>

# I'm Sorry Bills Fans

Each Type of QB WAR by Season, 2015-2017  
Highlighted = Tyrod Taylor



Good luck with Josh Allen!

# Recap and Future of nflWAR

Properly evaluating every play with with multinomial logistic regression model for EP and GAM for WP

Multilevel modeling provides an intuitive way for estimating player effects and **can be extended with data containing every player on the field for every play**

**Estimate the uncertainty** in the different types of iPA to generate intervals of WAR values

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Properly evaluating every play with with multinomial logistic regression model for EP and GAM for WP

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**Estimate the uncertainty** in the different types of iPA to generate intervals of WAR values

**Naive to assume player has same effect for every play!**

Refine the definition of replacement-level,  
e.g. what about down specific players? QBs that rush more?

**#GIVEMETRACKINGDATA**

# Future of Football Analytics

- **Brian Burke** (@bburkeESPN): father of modern football analytics - <http://www.advancedfootballanalytics.com/>
- **Josh Hermsmeyer** (@friscojosh): air yards, player stability, routes, etc - keeps work accessible, great visualizations
- **Zachary Binney** (@zbinney\_NFLinj): NFL injury expert
- **Eric Eager** (@PFF\_EricEager): Pro Football Focus collects everything - just don't look at their barcharts...

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*...there is another...*

# A New Hope



**Michael Lopez (@StatsbyLopez)** NFL Director of Data & Analytics

# Carnegie Mellon Sports Analytics Conference



**Clear your calendars for Oct 19-20th!**

**And visit <https://cmusportsanalytics.com/conference2018.html>**  
**for more information! #CMSAC18**

# Acknowledgements

**Max Horowitz** for creating `nflscrapR`

**Sam Ventura** for advising every step in the process

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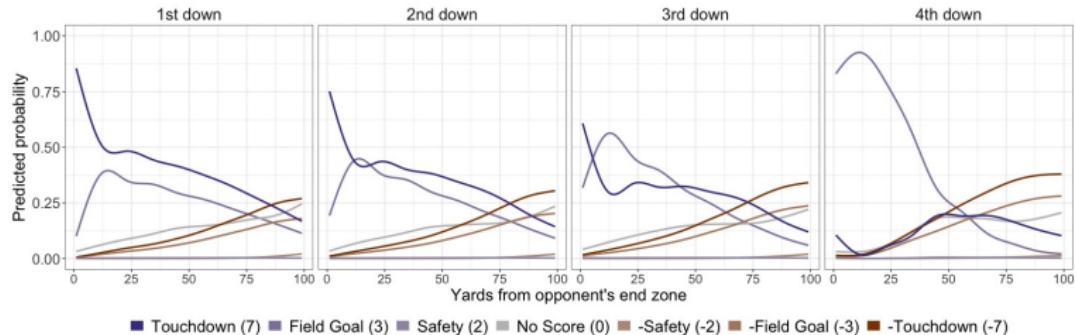
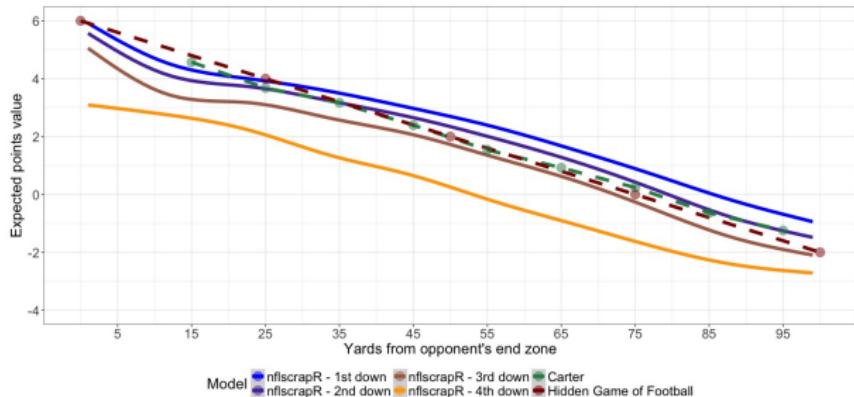
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**Thanks for your attention!**

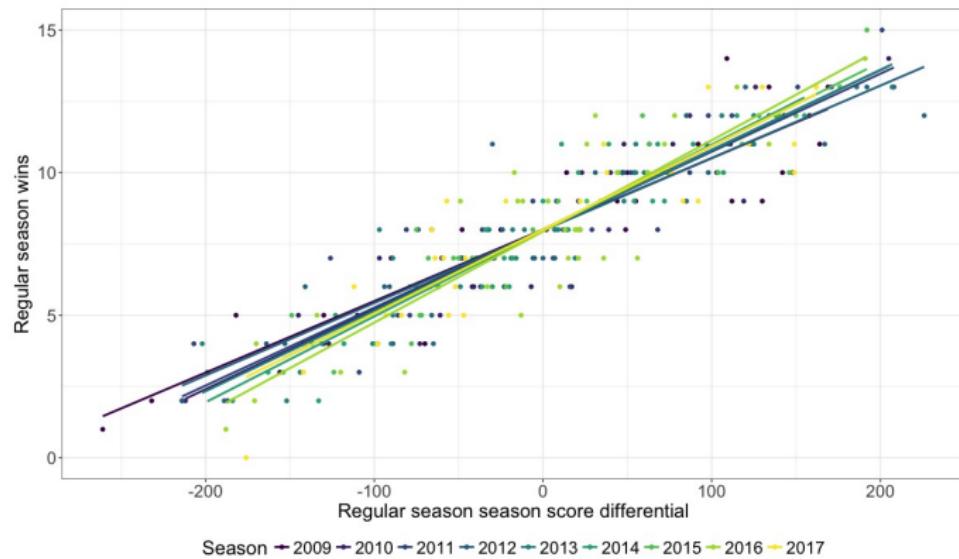
*No barcharts were harmed in the making of this presentation.*

# Expected Points Relationships



# Convert to Wins

“Wins & Point Differential in the NFL” - (Zhou & Ventura, 2017)  
(CMU Statistics & Data Science **freshman** research project)



## Relative to Replacement Level

Following an approach similar to **openWAR** (Baumer et al., 2015), defining replacement level based on roster

For each position sort by number of attempts, separate replacement level for rushing and receiving

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$$\text{Player } i's \text{ } iPAA_{i,\text{total}} = iPAA_{i,\text{rush}} + iPAA_{i,\text{air}} + iPAA_{i,\text{yac}}$$

Creates a replacement-level iPAA that “shadows” a player’s performance, denote as  $iPAA_i^{\text{replacement}}$

Player  $i$ 's **individual points above replacement (iPAR)** as:

$$iPAR_i = iPAA_{i,\text{total}} - iPAA_{i,\text{total}}^{\text{replacement}}$$

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